

$$6(7) = 42$$

$$65^2 = 4225$$



SQUARING OF SIX AND SEVEN DIGIT NUMBERS

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Abstract :

There are different methods for squaring of numbers .In this paper result of squaring of six and seven digit numbers are discussed.

Keywords: Squaring , Digits

INTRODUCTION:

Squaring of Two and Three digit numbers is given bt J.Trachtenberg[1]. Also Squaring of four and five digit numbers is given and the result is also generalized in [2].Here same logic is used for squaring of six and seven digit numbers.

Preliminaries: If b_0, b_1 are digits where $b_1 \neq 0$ then

$$(b_1 b_0)^2 = 10^2 b_1^2 + 10 (2 b_1 b_0) + b_0^2$$

$$\begin{aligned} \text{Ex. } (69)^2 &= (36)(108)(81) \\ &= (36)(116)(1) \\ &= (47)(61) \\ &= 4761 \end{aligned}$$

Step I : Result for six digit numbers

If $b_5, b_4, b_3, b_2, b_1, b_0$ are six digits with $b_5 \neq 0$
Then

$$\begin{aligned}
 (b_5b_4b_3b_2b_1b_0)^2 &= (10^5 b_5+10^4 b_4+10^3 b_3+10^2 b_2+10 b_1+ b_0)^2 \\
 &= (10^5 b_5+10^4 b_4+10^3 b_3)^2 + (10^2 b_2+10 b_1+ b_0)^2 + 2 (10^5 b_5+10^4 b_4+10^3 b_3) \\
 &\quad (10^2 b_2+10 b_1+ b_0) \\
 &= (10^5 b_5+10^4 b_4)^2 + 10^6 b_3^2 +2(10^5 b_5+10^4 b_4) 10^3 b_3 + (10^2 b_2+10 b_1)^2 + b_0^2 \\
 &\quad + 2 (10^2 b_2+10 b_1) b_0 + 2 \cdot 10^7 b_5 b_2 + 2 \cdot 10^6 b_5 b_1 + 2 \cdot 10^5 b_5 b_0 + 2 \cdot 10^6 b_4 b_2 \\
 &\quad + 2 \cdot 10^5 b_4 b_1 + 2 \cdot 10^4 b_4 b_0 + 2 \cdot 10^5 b_3 b_2 + 2 \cdot 10^4 b_3 b_1 + 2 \cdot 10^3 b_3 b_0 \\
 &= 10^{10} b_5^2 + 10^8 b_4^2 + 2 \cdot 10^9 b_5 b_4 + 10^6 b_3^2 + 2 \cdot 10^8 b_5 b_3 + 2 \cdot 10^7 b_4 b_3 + 10^4 b_2^2 \\
 &\quad + 10^2 b_1^2 + 2 \cdot 10^3 b_2 b_1 + b_0^2 + 2 \cdot 10^2 b_2 b_0 + 2 \cdot 10 b_1 b_0 + 2 \cdot 10^7 b_5 b_2 + 2 \cdot 10^6 \\
 &\quad b_5 b_1 + 2 \cdot 10^5 b_5 b_0 + 2 \cdot 10^6 b_4 b_2 + 2 \cdot 10^5 b_4 b_1 + 2 \cdot 10^4 b_4 b_0 + 2 \cdot 10^5 b_3 b_2 + \\
 &\quad 2 \cdot 10^4 b_3 b_1 + 2 \cdot 10^3 b_3 b_0 \\
 &= 10^{10} b_5^2 + 10^9 (2 b_5 b_4) + 10^8 (b_4^2 + 2 b_5 b_3) + 10^7 (2 b_4 b_3 + 2 b_5 b_2) + \\
 &\quad 10^6 (b_3^2 + 2 b_5 b_1 + 2 b_4 b_2) + 10^5 (2 b_5 b_0 + 2 b_4 b_1 + 2 b_3 b_2) + \\
 &\quad 10^4 (b_2^2 + 2 b_3 b_1 + 2 b_4 b_0) + 10^3 (2 b_2 b_1 + 2 b_3 b_0) + 10^2 (b_1^2 + 2 b_2 b_0) + \\
 &\quad 2 \cdot 10 b_1 b_0 + b_0^2
 \end{aligned}$$

Step II : Result for seven digit numbers

If $b_6, b_5, b_4, b_3, b_2, b_1, b_0$ are seven digits with $b_6 \neq 0$

Then

$$\begin{aligned}
 (b_6b_5b_4b_3b_2b_1b_0)^2 &= (10^6 b_6 + 10^5 b_5+10^4 b_4+10^3 b_3+10^2 b_2+10 b_1+ b_0)^2 \\
 &= (10^6 b_6 + 10^5 b_5+10^4 b_4+10^3 b_3)^2 + (10^2 b_2+10 b_1+ b_0)^2 + \\
 &\quad 2 (10^6 b_6 + 10^5 b_5+10^4 b_4+10^3 b_3) (10^2 b_2+10 b_1+ b_0) \\
 &= (10^6 b_6 + 10^5 b_5)^2 + (10^4 b_4 + 10^3 b_3)^2 + 2(10^6 b_6+10^5 b_5) \\
 &\quad (10^4 b_4+10^3 b_3) + (10^2 b_2+10 b_1)^2 + b_0^2 + 2 (10^2 b_2+10 b_1) b_0 + \\
 &\quad 2 (10^6 b_6 + 10^5 b_5+10^4 b_4+10^3 b_3) (10^2 b_2+10 b_1+ b_0) \\
 &= 10^{12} b_6^2 + 10^{10} b_5^2 + 2 \cdot 10^{11} b_6 b_5 + 10^8 b_4^2 + 10^6 b_3^2 + 2 \cdot 10^7 b_4 b_3 + \\
 &\quad 2 \cdot 10^{10} b_6 b_4 + 2 \cdot 10^9 b_6 b_3 + 2 \cdot 10^9 b_5 b_4 + 2 \cdot 10^8 b_5 b_3 + 10^4 b_2^2 + \\
 &\quad 10^2 b_1^2 + 2 \cdot 10^3 b_2 b_1 + b_0^2 + 2 \cdot 10^2 b_2 b_0 + 2 \cdot 10 b_1 b_0 + 2 \cdot 10^8 b_6 b_2 + \\
 &\quad 2 \cdot 10^7 b_6 b_1 + 2 \cdot 10^6 b_6 b_0 + 2 \cdot 10^7 b_5 b_2 + 2 \cdot 10^6 b_5 b_1 + 2 \cdot 10^5 b_5 b_0 + \\
 &\quad 2 \cdot 10^6 b_4 b_2 + 2 \cdot 10^5 b_4 b_1 + 2 \cdot 10^4 b_4 b_0 + 2 \cdot 10^5 b_3 b_2 + 2 \cdot 10^4 b_3 b_1 + \\
 &\quad 2 \cdot 10^3 b_3 b_0 \\
 &= 10^{12} b_6^2 + 10^{11} (2 \cdot b_6 b_5) + 10^{10} (b_5^2 + 2 \cdot b_6 b_4) + 10^9 (2 \cdot b_6 b_3 + 2 \cdot b_5 b_4) \\
 &\quad + 10^8 (b_4^2 + 2 \cdot b_5 b_3 + 2 \cdot b_6 b_2) + 10^7 (2 \cdot b_4 b_3 + 2 \cdot b_6 b_1 + 2 \cdot b_5 b_2) + \\
 &\quad 10^6 (b_3^2 + 2 \cdot b_6 b_0 + 2 \cdot b_5 b_1 + 2 \cdot b_4 b_2) + 10^5 (2 \cdot b_5 b_0 + 2 \cdot b_4 b_1 + 2 \cdot b_3 b_2) \\
 &\quad + 10^4 (b_2^2 + 2 \cdot b_4 b_0 + 2 \cdot b_3 b_1) + 10^3 (2 \cdot b_2 b_1 + 2 \cdot b_3 b_0) + \\
 &\quad 10^2 (b_1^2 + 2 \cdot b_2 b_0) + 10 (2 b_1 b_0) + b_0^2
 \end{aligned}$$

Examples : 1] Now We find the square of six digit number 324571
 $(324571)^2$

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$$\begin{aligned} &= (9)(2.3.2)(4+2.3.4)(2.2.4+2.3.5)(16+2.3.7+2.2.5)(2.3.1+2.2.7+2.4.5) \\ &\quad (25+2.4.7+2.2.1)(2.5.7+2.4..1)(49+2.5.1)(2(7.1))(1) \\ &= (9)(12)(28)(46)(78)(74)(85)(78)(59)(14)(1) \\ &= (9)(12)(28)(46)(78)(74)(85)(78)(60) 41 \\ &= (9)(12)(28)(46)(78)(74)(85)(84) 041 \\ &= (9)(12)(28)(46)(78)(74)(93) 4041 \\ &= (9)(12)(28)(46)(86) 334041 \\ &= (9)(12)(28) (54) 6334041 \\ &= (9)(12)(33) 46334041 \\ &= (9)(15) 346334041 \\ &= (10) 5346334041 \\ &= 105346334041 \end{aligned}$$

2] Now We find the square of seven digit number 2343562

$$(2343562)^2 =$$

$$\begin{aligned} &(4)(2.2.3)(9+2.2.4)(2.2.3+2.3.4)(16+2.3.3+2.2.5)(2.4.3+2.2.6+2.3.5)(9+2.2.2+2.3.6+2.4.5) \\ &(2.3.2+2.4.6+2.3.5)(25+2.4.2+2.3.6)(2.5.6+2.3.2)(36+2.5.2)(2.6.2)(4) \\ &= (4)(12)(25)(36)(54)(78)(93)(90)(77)(72)(56)(24)(4) \\ &= (4)(12)(25)(36)(54)(78)(93)(90)(77)(72)(58) 44 \\ &= (4)(12)(25)(36)(54)(78)(93)(90)(77)(77) 844 \\ &= (4)(12)(25)(36)(54)(78)(93)(90)(84) 7844 \\ &= (4)(12)(25)(36)(54)(78)(93)(98) 47844 \\ &= (4)(12)(25)(36)(54)(78)(102) 847844 \\ &= (4)(12)(25)(36)(54)(88) 2847844 \\ &= (4)(12)(25)(36)(62) 82847844 \\ &= (4)(12)(25)(42) 282847844 \\ &= (4)(12)(29) 2282847844 \end{aligned}$$

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$$= (4)(14) \ 92282847844$$

$$= (5) \ 492282847844$$

$$= 5492282847844$$

CONCLUSION:

We have obtained the result for six and seven digit numbers which can be extended for more digits and for solving the examples result is obtained by capping the numbers.

6. REFERENCES :

[1] Ann Cutler and Rudolph macshane. The Trachtenberg Speed System of basic mathematics , 17 Impression Rupa& Co. new delhi1998

[2] Squaring of Numbers –C.R. Bembalkar And D.B.Dhaigude , The Bulletin Of MMS Dec.2000